

Wide-Area Monitoring and Control Using PMUs for Power System Stability

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Abstract— *Traditional power system security assessment methods, primarily based on SCADA data and offline studies conducted well in advance of real-time operations, are increasingly inadequate for modern grid requirements, as they fail to accurately anticipate the diverse and dynamic conditions encountered by system operators. To address these limitations, advanced technologies such as Phasor Measurement Units (PMUs), which utilize synchrophasor measurements, enable precise, high-resolution, and real-time monitoring of actual system states. These technologies support enhanced operational awareness by facilitating continuous monitoring, real-time assessment, and automated control actions to prevent or mitigate system disturbances. PMU-based applications provide operators with critical tools to detect and avoid voltage and dynamic instability, as well as to monitor generator responses during significant frequency deviations. This paper highlights the benefits of PMU deployment in selected real-time applications, reviews ongoing pilot projects and global implementation experiences, and proposes both short-term and long-term roadmaps for the future development and integration of synchrophasor-based systems..*

Keywords— “Phasor Measurement Units (PMU)”, “Real-Time Monitoring”, “Wide Area Monitoring Systems (WAMS)”, “SCADA Limitations”, “Dynamic Stability”

I. INTRODUCTION

Rising grid congestion and large-scale disturbances across power systems worldwide have highlighted the need for enhanced operational frameworks, particularly through the adoption of Wide Area Monitoring, Protection, and Control (WAMPAC) systems as a cost-effective solution for improving system planning, operation, maintenance, and energy trading. WAMPAC systems leverage recent advancements in sensing, communication, computing, visualization, and advanced algorithms to deliver improved situational awareness and control capabilities. A key enabler of these systems is synchronized phasor measurement technology, which plays a crucial role in providing accurate, time-aligned system data. The technological infrastructure required to support such applications—including Phasor Measurement Units (PMUs), phasor data concentrators, data acquisition systems, communication networks, and EMS/SCADA and market operation platforms—is already well established. Although time synchronization itself is not a new concept in power systems, its precision has significantly evolved with technological progress, transitioning from minute-level to microsecond-level accuracy. Looking ahead, it is anticipated that high-precision time synchronization will become a standard feature across all metering devices, with time-stamped measurements forming an integral part of future power system monitoring and control.

Phasor measurement technology for power system applications emerged in the late 1980s, with the first commercial products introduced in the early 1990s, and has since evolved into a widely adopted solution supported by multiple vendors. Today, Phasor Measurement Units (PMUs), along with Phasor Data Concentrators (PDCs), are deployed globally, with large-scale initiatives such as the Eastern Interconnection Phasor Project (EIPP) further accelerating their implementation. PMUs are currently the most advanced time-synchronized measurement tools available for wide-area monitoring, enabled by significant progress in computing technologies and the availability of precise GPS-based time synchronization. However, realizing their full potential requires parallel advancements in complementary domains. Notably, improvements in communication infrastructure have enabled faster and more reliable transmission of high-resolution PMU data from remote locations to centralized control centers. Despite these advancements, challenges remain in measurement accuracy due to limitations of conventional instrument transformers, which influence the quality of input signals to PMUs; although newer technologies such as optical transducers offer improvements, they often come at higher costs. Addressing these issues necessitates enhanced testing procedures, better characterization of dynamic response, adoption of digitally compatible measurement interfaces, and the use of software-based error correction techniques leveraging measurement redundancy. Furthermore, the development

of robust applications and analytical tools to process PMU data remains critical, as effective utilization depends on both advanced algorithms and skilled operators. While significant progress has been made by academia, industry, and utilities in developing such applications, including real-time monitoring, alarm generation, and control functions, the successful integration of PMU data into control centers—presented through intuitive graphical interfaces—continues to be an essential step toward maximizing the benefits of this technology.

II. OVERVIEW OF WAMPAC ARCHITECTURE

2.1 Phasor Measurement Units (PMUs)

A Phasor Measurement Unit (PMU) installed at a substation measures voltage and current phasors with highly precise time-stamping, typically accurate to the microsecond level, indicating the exact instant at which each measurement is recorded. In addition to phasor data, PMUs compute key electrical parameters such as active and reactive power (MW/MVAR) as well as system frequency. These measurements are transmitted at high reporting rates, generally ranging from 20 to 60 samples per second, enabling detailed and real-time monitoring of power system dynamics.

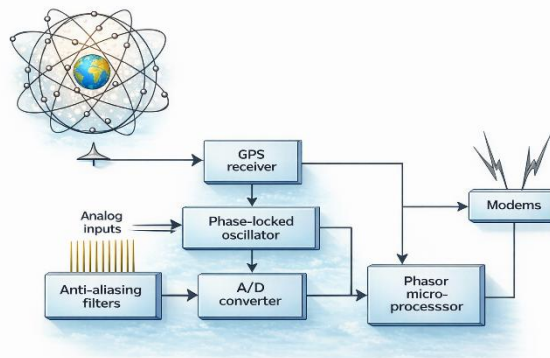


Fig.2.1 Phasor Measurement Unit Architecture

Phasor Measurement Unit (PMU) technology is highly effective for tracking power system dynamics in real time, offering a significant advantage over conventional SCADA/EMS systems, which typically operate with refresh rates ranging from seconds to minutes. In a typical implementation, each utility deploys a Phasor Data Concentrator (PDC) to collect, align, and synchronize data from multiple PMUs based on precise time stamps. The aggregated data from individual utility PDCs are then transmitted to a central facility, where measurements from different regions are further synchronized across the entire grid. Advanced applications at the central facility utilize this time-aligned data to provide a comprehensive, grid-wide snapshot at sub-second intervals, enabling accurate and continuous monitoring of system dynamics.

III. WAMPAC SYSTEM ARCHITECTURE

Emerging technologies for real-time wide-area monitoring, control, and protection are primarily focused on three key objectives: enhancing system resilience against disturbances, increasing transmission capacity, and improving asset utilization. Modern power systems, traditionally operated under the N-1 reliability criterion, are increasingly challenged by market-driven environments that limit control over generation dispatch, often forcing operation under less secure N-0 conditions. This shift necessitates the adoption of advanced Wide Area Monitoring, Protection, and Control (WAMPAC) systems to manage higher operational risks and prevent cascading failures and blackouts. Additionally, these technologies aim to alleviate congestion in transmission corridors—particularly between interconnected electricity markets—and to optimize the utilization of transmission infrastructure through improved planning, operation, and protection strategies. Over the past two decades, the development and deployment of phasor measurement technology have demonstrated significant effectiveness in addressing these challenges, particularly in enabling real-time wide-area monitoring and analysis, coordinated control, and adaptive protection. Successful implementation of such systems requires robust hardware and software platforms, reliable communication architectures, advanced signal processing capabilities, and specialized applications for real-time operations. These include tools for system monitoring by reliability coordinators, diagnostic support for operational engineers, continuous and event-based data archiving for post-event analysis, and coordinated adaptive protection schemes. Consequently, multi-layered architectures—typically comprising four layers—are emerging as the most effective framework for implementing comprehensive WAMPAC systems.

▪ **Layer 1, Phasor Data Acquisition**

Consists of Phasor Measurement Units (PMUs) and Digital Fault Recorders (DFRs) installed at substations to measure key electrical parameters such as voltage, current, and system frequency. The phasor measurement process involves extracting positive-sequence components at the fundamental frequency from the measured voltage and current waveforms. In addition to continuous monitoring, PMUs can be configured to capture and store data based on specific event triggers, such as under-voltage, over-voltage, or abnormal frequency conditions, thereby enabling detailed analysis of system disturbances.

▪ **Layer 2, Phasor Data Management**

Involves the use of Phasor Data Concentrators (PDCs) to collect and manage data from multiple PMUs as well as from other upstream or downstream PDCs. The PDC aligns and correlates the incoming time-synchronized measurements into a unified and coherent dataset, ensuring consistency across the system. This processed data is then streamed in real time to various applications through an application data buffer, enabling efficient access for monitoring, analysis, and control functions.

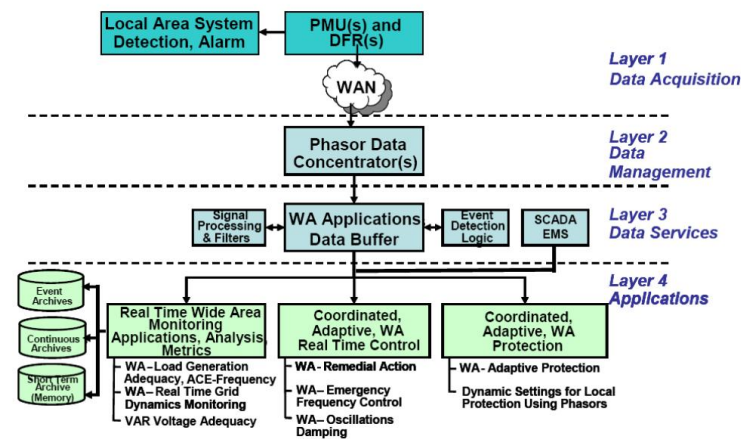


Fig. 3.1 WAMPAC system architecture

▪ **Layer 3, Data Services**

Comprises the set of essential services responsible for delivering phasor data to various applications in an efficient and usable manner. This layer ensures that data is formatted appropriately to meet the specific requirements of different applications while maintaining high-speed processing to allow sufficient time for application execution within the sampling interval. In addition, it plays a critical role in system management by continuously monitoring incoming data streams for issues such as data loss, errors, and synchronization problems, thereby ensuring data integrity, reliability, and overall system performance.

▪ **Layer 4, Applications**

Represents the highest level of the architecture, where processed and time-synchronized phasor data is utilized for advanced operational functions. This layer primarily focuses on three key application areas: real-time wide-area monitoring and analysis, which provides comprehensive visibility of grid conditions; real-time wide-area control, which enables coordinated control actions to maintain system stability; and real-time wide-area adaptive protection, which ensures rapid and intelligent protection responses based on dynamic system conditions. Together, these applications enhance the reliability, security, and efficiency of modern power system operations.

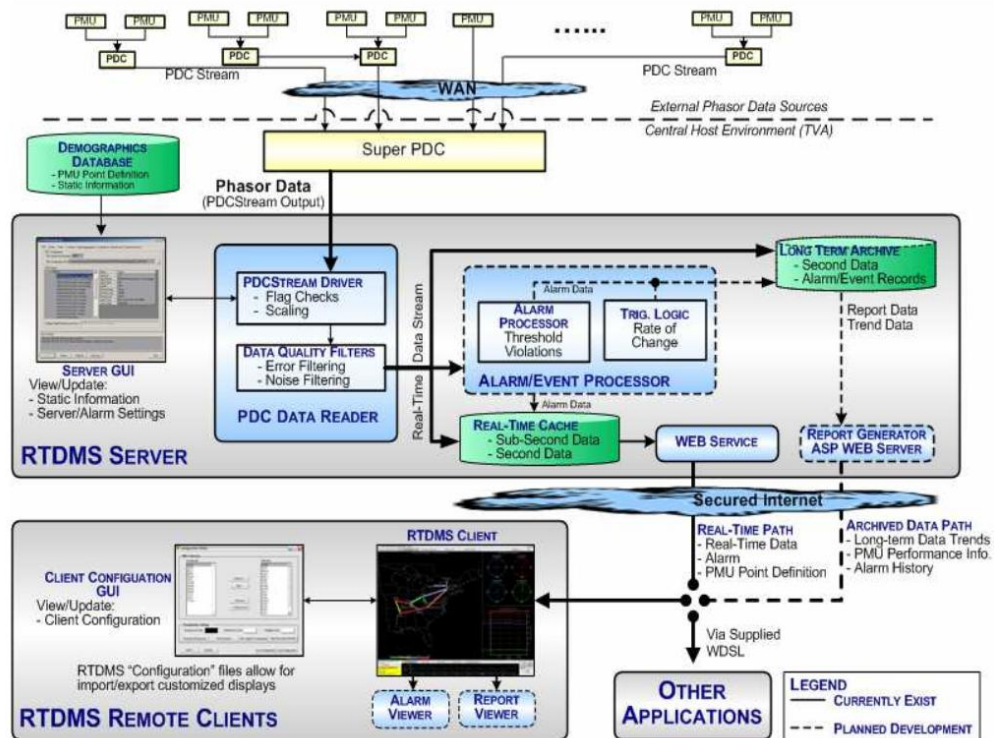


Fig. 3.2 WAMPAC system IT architecture

3.1 Benefits Of Using PMUS

Real-time monitoring and control

- The primary objective of real-time monitoring is to provide system operators with continuous, online awareness of power system conditions, thereby improving operational efficiency during normal conditions and enabling timely detection, anticipation, and mitigation of issues during abnormal situations.
- Currently, Energy Management System (EMS) security monitoring relies on State Estimator outputs, which use system models and SCADA telemetry data to compute voltage magnitudes and phase angles across the network at intervals of several seconds.
- The introduction of time-synchronized measurement devices, such as PMUs, enables direct measurement of system states rather than relying solely on estimation techniques, although full-scale deployment may not yet be economically feasible and is expected to be implemented progressively.
- Existing commercial solutions support a limited number of synchronized measurement devices; however, their capability to manage large-scale deployments involving hundreds of devices remains to be fully validated.
- One immediate advantage of PMU implementation is improved situational awareness, allowing not only local operators but also neighboring control areas to be informed of emerging grid stress conditions.
- Real-time observation of voltage angle differences allows operators to refine conservative limits derived from planning and offline studies, enabling more accurate and dynamic assessment of system stability.
- Continuous monitoring using PMUs facilitates operation of transmission corridors closer to actual stability limits while maintaining system security, thereby reducing unnecessary safety margins.
- Operating closer to true system limits can significantly reduce the need for costly infrastructure upgrades by maximizing the utilization of existing transmission assets.
- Enhanced confidence in system stability also enables the development of adaptive protection schemes that respond dynamically to real-time system conditions, improving both local and wide-area protection performance.

- The identification and analysis of inter-area oscillation modes using PMU data contribute to the refinement of dynamic system models, increasing their accuracy and reliability for system studies.
- Improved dynamic models can be used to optimize the placement and tuning of power system stabilizers, enhancing overall system stability.
- From a financial perspective, PMU-based voltage stability monitoring offers benefits in congestion management by allowing operators to use actual system limits instead of conservative estimates, thereby increasing permissible power transfer capacity.

Another important benefit of PMU-based applications lies in blackout prevention, which, although associated with low-probability events, carries extremely high economic and operational consequences; however, accurately quantifying these benefits requires detailed, system-specific studies that consider grid characteristics and the expected reliability of the implemented schemes. Voltage instability, a major contributor to such events, is typically characterized by low voltage profiles, high reactive power flows, insufficient reactive power support, and heavily loaded system conditions. Voltage collapse often occurs suddenly following a symptomatic phase that may last from a few seconds to several minutes or even hours, and is frequently triggered by rare single or multiple contingency events. The analysis of voltage collapse necessitates a combined approach using both static and dynamic methods, making it particularly well-suited for PMU-based monitoring and control systems. Unlike conventional monitoring tools, which often lack the capability to capture fast system dynamics, PMUs provide the high-resolution, time-synchronized measurements required for effective voltage stability assessment and protection.

Power System State Estimation

State Estimation (SE) is extensively utilized in transmission control centers and Independent System Operator (ISO) operations to complement real-time telemetered measurements for effective grid monitoring. It enables the assessment of network conditions that are not directly measured and provides a consistent and reliable estimate of the system state, which serves as a foundation for advanced real-time applications such as contingency analysis, constrained redispatch, Volt/VAR optimization, and congestion management. In addition, SE supports several ancillary functions, including bad data detection, parameter estimation, status identification, and external network modeling, though their practical adoption varies across the industry.

The integration of phasor measurement units (PMUs) into SE has been demonstrated in at least one successful deployment, with several pilot projects currently underway. From a computational perspective, incorporating PMU data into SE algorithms is relatively straightforward, except for challenges associated with reference bus selection. Despite its potential, practical experience with PMU-based SE remains limited. Nonetheless, ongoing research has introduced algorithmic enhancements, particularly in areas such as bad data detection and parameter estimation. PMUs also present an opportunity for ISO/RTO-level state estimation by improving the representation of boundary conditions for utility-level estimators.

PMUs offer several advantages to SE applications, including enhanced accuracy and robustness in bad data detection, faster numerical solutions due to the linear nature of measurements, and access to direct information about external network conditions. Additionally, the high sampling rates of PMUs enable the development of standalone SE solutions based entirely on PMU data, which can operate with higher temporal resolution and simplified linear formulations, as voltage magnitudes and phase angles are directly measured.

Furthermore, existing PMU communication infrastructure can potentially be leveraged to integrate data from compatible digital protection relays, thereby improving data redundancy and possibly reducing deployment costs. Another promising yet underexplored area is the development of three-phase or sequence-based state estimators derived from PMU data. Such approaches could provide valuable insights into phase unbalance, which may indicate grounding issues or equipment degradation. This potential warrants further investigation to assess its practical benefits and applicability in modern power systems.

Real-Time Congestion Management

Congestion management is a vital function carried out by power schedulers in day-ahead markets and by grid operators in real-time operations to ensure that electricity demand is met economically without exceeding transmission constraints. In real-time applications, its primary objective is to maintain power flows within the secure transfer limits of transmission lines and corridors through optimal and cost-effective dispatch adjustments. Traditionally, congestion management relies on comparing actual power flows with Nominal Transfer Capability (NTC), which is determined through offline studies considering thermal, voltage, and stability

constraints. However, these offline assessments are often based on conservative assumptions, leading to overly restrictive limits, underutilization of transmission capacity, and increased operational costs.

The integration of phasor measurement units (PMUs), which provide synchronized and high-precision system measurements, offers significant potential to enhance real-time congestion management. By enabling more accurate estimation of power flows and transmission limits, PMUs facilitate improved calculation of real-time transfer capability (RTC), particularly for voltage- and stability-constrained paths. This allows system operators greater flexibility in managing congestion, reduces unnecessary curtailments, and supports more efficient dispatch decisions. Consequently, the use of PMU data can lead to better utilization of existing infrastructure, lower operational costs, and overall economic benefits for both utilities and consumers.

Benchmarking, validation and fine-tuning of system models

The objective of model verification and Parameter Estimation (PE) is to detect inaccuracies in power system modeling data—including network, generator, and load parameters—and to derive improved estimates for these values. Model development is generally a labor-intensive process that relies heavily on engineering judgment, making it susceptible to human error. Once inaccuracies are introduced into the modeling database, they can be difficult to identify and may persist undetected for extended periods.

The adoption of phasor measurement unit (PMU)-based tools and methodologies provides a robust approach for improving model accuracy. By delivering precise, time-synchronized measurements from multiple locations across the power system, PMUs enable more effective detection of modeling errors and support the refinement of system models used in both online and offline applications, such as power flow analysis, stability studies, short-circuit analysis, optimal power flow (OPF), security assessment, congestion management, and dynamic response evaluation. For steady-state models, Energy Management System (EMS) vendors have developed algorithms for identifying discrepancies and estimating corrected parameters—a process known as parameter estimation. The integration of high-accuracy PMU data significantly enhances the performance of these algorithms, particularly in estimating parameters such as line impedances, admittances, and transformer tap settings. In practice, PMU-based techniques for transmission line impedance estimation have already been commercialized and implemented in regions such as Europe. However, the validation and tuning of dynamic and oscillatory models remain more complex, typically requiring detailed analysis of system responses to both planned and unplanned disturbances.

Post-Disturbance Analysis

The objective of post-mortem or post-disturbance analysis is to reconstruct the sequence of events following a power system disturbance. Traditionally, this process involves the collection and examination of data from multiple recorders distributed across the grid. Although such recording devices have long been used in the industry, their lack of time synchronization makes it difficult and time-consuming to accurately establish the chronological order of events. The introduction of Global Positioning System (GPS)-based time synchronization has significantly improved this process, particularly with the advent of advanced devices such as phasor measurement units (PMUs). The deployment of these technologies has been strongly advocated following major disturbances, including the 2003 Northeast US and Italian blackouts.

Unlike real-time wide-area monitoring, protection, and control (WAMPAC) systems, post-disturbance analysis systems do not require stringent communication network performance, as data transmission delays are acceptable. Data can be locally stored at substations and retrieved centrally as needed. However, the increasing volume of recorded data necessitates the development of advanced analytical tools to assist engineers in efficiently extracting critical insights. Several utilities, particularly in the United States, have already implemented GPS-synchronized recording devices, significantly reducing disturbance analysis time from hours to seconds. In Europe, the 2003 Italian blackout led to widespread PMU deployment, which not only improved time synchronization but also enabled additional capabilities such as real-time monitoring of phase angle differences and frequency oscillations across interconnected grid regions.

Power-system restoration

During power system restoration, operators frequently face significant standing phase angle (SPA) differences across circuit breakers connecting adjacent substations. Closing a breaker under such conditions can impose severe electrical stress on the system, potentially leading to equipment damage or even triggering a subsequent outage. Phasor measurement units (PMUs), with their capability for real-time and precise phase angle monitoring, are well suited to support operators by providing accurate situational awareness during restoration processes.

Practical experience has highlighted the importance of phase-angle monitoring in ensuring safe system recovery. In high-pressure restoration scenarios, PMU-based monitoring serves as a critical decision-support tool, enabling operators to assess synchronization conditions before breaker closure. By improving visibility into

system conditions, PMUs can enhance operational safety and significantly reduce the time required for system restoration.

Protection and Control Applications for Distributed Generation

A significant portion of the projected annual generation capacity expansion—estimated at approximately 15 GW per year in the United States—is expected to be met through distributed generation (DG). Factors such as evolving pricing structures, increased competition in the electricity retail market, and the operational advantages of locating generation close to load centers are driving the rapid growth of DG technologies. Studies by EPRI suggest that DG could account for nearly 25% of new generation capacity and potentially represent up to 20% of the overall electric utility market. In this context, phasor measurement unit (PMU) technology demonstrates considerable potential for effective monitoring and controlled islanding of DG systems and microgrids. However, the development of cost-effective PMU solutions remains essential to enable widespread adoption and integration.

Overload Monitoring and Dynamic Rating

A wide range of sensors, devices, and associated software systems are available to utilities for monitoring power system equipment. Phasor measurement units (PMUs) contribute to this capability by providing high-resolution, time-synchronized data for system monitoring. Although PMU-based approaches to overload monitoring and dynamic line rating may not fully replicate the advanced features of dedicated equipment monitoring systems, a key advantage lies in their multifunctionality, as the same PMU infrastructure can support multiple applications.

Currently, one of the primary commercial applications of PMU technology is in the monitoring of overhead transmission lines. By installing PMUs at both ends of a line, real-time measurements can be used to estimate line impedance, which in turn enables the calculation of the average conductor temperature. However, this approach has certain limitations, as it does not provide detailed information about localized conditions such as hotspots, conductor sag, or critical spans along the line.

Adaptive Protection

Synchronized phasor measurements enable the development of adaptive protection schemes in which relays can dynamically adjust their characteristics in response to prevailing power system conditions, thereby improving overall performance. Traditional protection systems operate based on fixed settings derived from assumed system conditions, which may not accurately reflect real-time scenarios. In contrast, adaptive relaying recognizes the need for flexibility in relay behavior. With the advancement of digital relays—characterized by software-based functionality and communication capabilities—protection settings can be modified in real time through supervisory control systems or remote measurements. Since its large-scale introduction in the late 1980s, adaptive relaying has gained importance due to tighter operating margins and increased emphasis on economic efficiency in power system operation.

The integration of phasor measurement unit (PMU) data further enhances adaptive protection by enabling more accurate and responsive relay operation. Applications include improved performance of out-of-step protection, line relaying, adaptive reclosing, and achieving an optimal balance between system security and dependability under varying conditions. Additionally, PMUs offer significant advantages in fault location by providing precise measurements of transmission line impedance, a critical parameter for accurate fault analysis. The use of synchronized data from both ends of a transmission line allows for direct fault calculation, thereby reducing errors in fault location and minimizing the time required for system diagnosis and restoration.

Planned Power System Separation

The direct utilization of phasor measurement unit (PMU) data has the potential to significantly enhance system performance in planned power system separation. System separation into electrically isolated islands is typically employed as a last-resort measure during severe electromechanical instability, where maintaining system integrity becomes impossible. In such situations, controlled and intentional islanding is preferred over uncontrolled separation, with the objective of forming stable subsystems that can later be reconnected when conditions permit. Ideally, each island should maintain a balance between generation and load; however, achieving this balance may require additional corrective actions such as generator tripping or load shedding.

Conventional approaches to system separation, including out-of-step relaying and remedial action schemes, rely on predefined system conditions derived from offline studies. These methods are based on assumptions regarding system loading, topology, and contingencies, which may not accurately represent real-time operating conditions. As a result, their performance can be suboptimal or even inappropriate under actual system states,

potentially exacerbating instability. In contrast, PMU-based approaches leverage real-time, synchronized measurements to improve decision-making. They enable more accurate detection of impending instability and identification of generator groups at risk of losing synchronism, while also allowing dynamic determination of optimal islanding boundaries based on current system conditions. This real-time adaptability enhances the effectiveness and reliability of planned system separation strategies.

IV. CONCLUSIONS

In conclusion, the effective application of power system technologies requires continuous learning, strong technical understanding, and practical experience. Advanced tools such as phasor measurement units (PMUs) have proven their value in enhancing system monitoring, improving reliability, and providing deeper insight into overall grid behavior when used within their operational limits. However, the successful implementation of phasor measurement technology demands substantial investment and commitment from utilities and system operators, including system studies, infrastructure upgrades, maintenance, and workforce training. Therefore, the development of a clear and structured roadmap is essential to guide stakeholders in prioritizing applications based on their benefits, costs, and technological progress, while also supporting the evaluation and improvement of existing systems and the exploration of new solutions for future power system challenges.

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